JOURNAL OF ALGEBRA **180,** 321–322 (1996)
ARTICLE NO. 0068

ERRATUM

Volume **175**, Number 3 (1995), in the article "On the Hilbert–Kunz Function and Koszul Homology," by M. Contessa, pages 757–766: On page 757, line 4 from the bottom should read "$A = K[[X_1, \dots, X_d]] \twoheadrightarrow R$, $X_i \mapsto x_i$, K being a coefficient field . . . ." On page 758, line 5 should read "the case where R is regular" and line 7 should read "By Monsky's results (cf. [8]), $l_R(M/(X_1^q, \dots, X_d^q)M)$." On page 759, line 1 should read "$l_R(M/(X_1, \dots, X_d)M = q^d \cdot (rkM)$ *and* $l_R(H_i(\underline{X}^q;\ M)) = 0$, $i \geq 1$," and line 19 should read "*the map* $H_i(X_j^{n_j};\ M) \xrightarrow{\alpha} H_i(X_j^{n_j};\ \overline{M})$ *is onto*." On page 760, line 5 should read "$R = k[[X_1, \dots, X_d]]$," line 20 should read "reflexive modules over $k[[X, Y]]$ are free," and line 27 should read "*Let* $0 \to T \to M \xrightarrow{\varphi} \overline{M} \to 0$ *be an exact sequence*." On page 761, lines 13–14 should read "the image of $\bar{u}$ in $T/(X^sT, Y^tT)$ is represented by $X^{s+1}a + Y^t(Xb) = X(X^sa + Y^tb)$," and line 22 should read "*where C is an integer* ≥ 0." On page 762, lines 1–3 should read "By dérissage we may assume $M = R/\mathfrak{P}$ with $\mathfrak{P}$ prime. When $\dim M \leq d - i$ the result follows from [10] (or [9, Lemma 2.6])," and line 25 should read "$H_1(X^{p^n};\ M)$ has length independent of n for $n \gg 0$." On page 763, line 12 should read "*Fix* $q_0 = p^{e_0}$," line 15 should read "*for all* $q \gg 0$, $X_1^{q-q_0}m_1 + X_2^{q-q_0}m_2 + \cdots + X_n^{q-q_0}m_n \in (X_1^q, \dots, X_n^q)$," line 23 should read "we get $\forall j,\ \forall t,\ m_j - X_j^{q_0}w_j \in (X_1^{q_t-q_0}, \dots, X_j^{q_t-q_0}, \dots, X_n^{q_t-q_0})F$," line 27 should read "In F we have $(m_1' - w_1, \dots, m_n' - w_n)$," and line 28 should read "Hence $(m_1', \dots, m_n') = (w_1, \dots, w_n) + \mathfrak{m}^{q_t}F^n \subseteq M^n + \mathfrak{m}^{q_t}F^n$." On page 764, the displayed equation should read

$$
\begin{aligned}
H_i(X^q;\ M)^* &\cong \operatorname{Tor}_i^R(R/\underline{X}^q,\ M)^* \\
&\cong H_i(F_\odot \otimes R/(\underline{X}^q)) \\
&\cong H_i(\operatorname{Hom}_R(F_\odot \otimes R/(\underline{X}^q), E)), \qquad \text{where } E = E(k) \\
&\cong H_i(\operatorname{Hom}_R(F_\odot, \operatorname{Hom}_R(R/(\underline{X}^q), E))) \\
&\cong H_i(\operatorname{Hom}_R(F_\odot, R/(\underline{X}^q))) \\
&\cong H_i(\operatorname{Hom}_R(F_\odot, R) \otimes R/(X^q)) \\
&= \operatorname{Tor}_{d-i}^R(M^\upsilon, R/(\underline{X}^q)) = H_{d-i}(\underline{X}^q;\ M^\upsilon).
\end{aligned}
$$

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Also on page 764, line 6 from the bottom should read "M_1 *is torsion-free*," and line 2 from the bottom should read "$H_{i+1}(\underline{X}_j^{n_j}; M) \to K_{i+1}(X_j^{n_j}; D) \xrightarrow{\vartheta} H_i(\underline{X}_j^{n_j}; (M_1) \to H_i(\underline{X}_j^{n_j}; M) \to .$" On page 765, lines 18–19 should read, "[One can ignore the finite length submodule of M, if there is one.]" and line 22 should read "M has a submodule M' which is a direct sum of cyclic modules...." On page 766, Ref. 8 should read "P. MONSKY, The Hilbert–Kunz Function, *Math. Ann.* **263** (1983), 43–49" and Ref. 11 should read "J. P. SERRE, "Algèbre locale: Multiplicités," 3rd ed., Lecture Notes in Math., Vol. 11, Springer-Verlag, New York/Berlin, 1975.